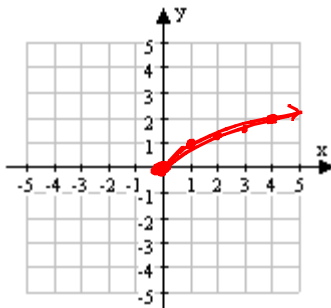


Consider the following EQUATIONS, make a table, plot the points, and graph what you think the graph looks like.

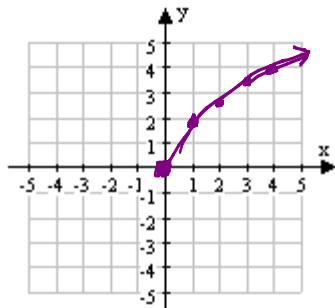
1.  $f(x) = \sqrt{x}$

x	y
-4	<del><math>\sqrt{-4} = 2i</math></del>
-1	<del><math>\sqrt{-1} = i</math></del>
0	$\sqrt{0} = 0$
1	$\sqrt{1} = 1$
2	$\sqrt{2} \approx 1.41$
3	$\sqrt{3} \approx 1.73$
4	$\sqrt{4} = 2$



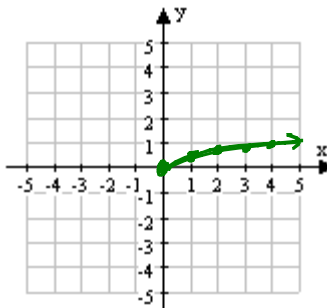
2.  $f(x) = 2\sqrt{x}$

x	y
-4	<del><math>2\sqrt{-4} = 2 \cdot 2i = 4i</math></del>
-1	<del><math>2\sqrt{-1} = 2i</math></del>
0	$2\sqrt{0} = 2 \cdot 0 = 0$
1	$2\sqrt{1} = 2 \cdot 1 = 2$
2	$2\sqrt{2} \approx 2.83$
3	$2\sqrt{3} \approx 3.46$
4	$2\sqrt{4} = 2 \cdot 2 = 4$



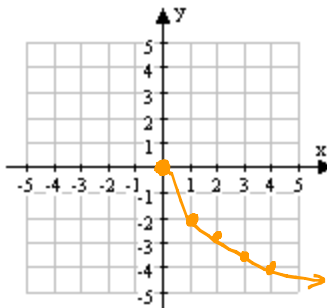
3.  $f(x) = 0.5\sqrt{x}$

x	y
-4	<del><math>0.5\sqrt{-4} = 0.5 \cdot 2i = i</math></del>
-1	<del><math>0.5\sqrt{-1} = 0.5i</math></del>
0	$0.5\sqrt{0} = 0.5 \cdot 0 = 0$
1	$0.5\sqrt{1} = 0.5 \cdot 1 = 0.5$
2	$0.5\sqrt{2} \approx 0.71$
3	$0.5\sqrt{3} \approx 0.87$
4	$0.5\sqrt{4} = 0.5 \cdot 2 = 1$



4.  $f(x) = -2\sqrt{x}$

x	y
-4	<del><math>-2\sqrt{-4} = -2 \cdot 2i = -4i</math></del>
-1	<del><math>-2\sqrt{-1} = -2i</math></del>
0	$-2\sqrt{0} = -2 \cdot 0 = 0$
1	$-2\sqrt{1} = -2 \cdot 1 = -2$
2	$-2\sqrt{2} \approx -2.83$
3	$-2\sqrt{3} \approx -3.46$
4	$-2\sqrt{4} = -2 \cdot 2 = -4$



5. What happens to the graph as the number in front of  $\sqrt{x}$  gets Larger? Close to Zero? Negative? \_\_\_\_\_

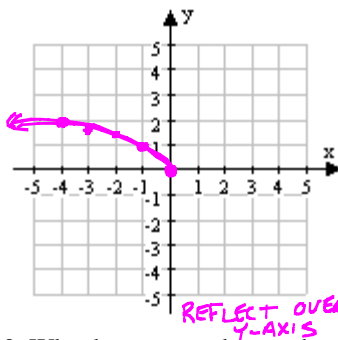
AS THE COEFFICIENT OF THE  $\sqrt{x}$  GETS LARGER THE GRAPH BECOMES VERTICALLY STRETCHED.

AS THE COEFFICIENT OF THE  $\sqrt{x}$  GETS CLOSER TO ZERO THE GRAPH BECOMES VERTICALLY COMPRESSED

WHEN THE COEFFICIENT OF  $\sqrt{x}$  IS NEGATIVE THE GRAPH IS FLIPPED OR REFLECTED OVER THE X-AXIS.

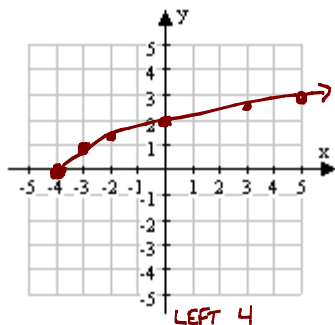
6.  $f(x) = \sqrt{-x}$

x	y
-4	$\sqrt{-(-4)} = \sqrt{4} = 2$
-3	$\sqrt{-(-3)} = \sqrt{3} \approx 1.73$
-2	$\sqrt{-(-2)} = \sqrt{2} \approx 1.41$
-1	$\sqrt{-(-1)} = \sqrt{1} = 1$
0	$\sqrt{-(-0)} = \sqrt{0} = 0$
1	<del><math>\sqrt{-1} = i</math></del>
4	<del><math>\sqrt{-4} = 2i</math></del>



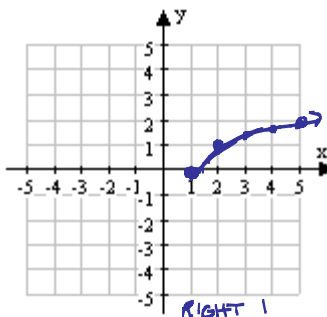
7.  $f(x) = \sqrt{x+4}$

x	y
-5	<del><math>\sqrt{-5+4} = \sqrt{-1} = i</math></del>
-4	$\sqrt{-4+4} = \sqrt{0} = 0$
-3	$\sqrt{-3+4} = \sqrt{1} = 1$
-2	$\sqrt{-2+4} = \sqrt{2} \approx 1.41$
0	$\sqrt{0+4} = \sqrt{4} = 2$
3	$\sqrt{3+4} = \sqrt{7} \approx 2.65$
5	$\sqrt{5+4} = \sqrt{9} = 3$



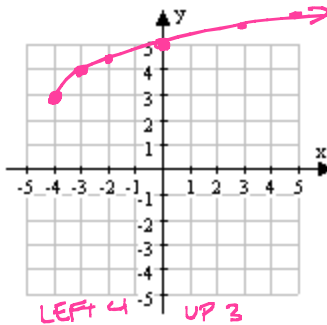
8.  $f(x) = \sqrt{x-1}$

x	y
-3	<del><math>\sqrt{-3-1} = \sqrt{-4} = 2i</math></del>
0	<del><math>\sqrt{0-1} = \sqrt{-1} = i</math></del>
1	$\sqrt{1-1} = \sqrt{0} = 0$
2	$\sqrt{2-1} = \sqrt{1} = 1$
3	$\sqrt{3-1} = \sqrt{2} \approx 1.41$
4	$\sqrt{4-1} = \sqrt{3} \approx 1.73$
5	$\sqrt{5-1} = \sqrt{4} = 2$



9.  $f(x) = \sqrt{x+4} + 3$

x	y
-5	<del><math>\sqrt{-5+4} + 3 = 3+i</math></del>
-4	$\sqrt{-4+4} + 3 = 3$
-3	$\sqrt{-3+4} + 3 = 4$
-2	$\sqrt{-2+4} + 3 \approx 4.41$
0	$\sqrt{0+4} + 3 = 5$
3	$\sqrt{3+4} + 3 \approx 5.65$
5	$\sqrt{5+4} + 3 = 6$



10. What happens to the graph as we add or subtract a number inside or outside the radical? \_\_\_\_\_

WHEN WE ADDED A NUMBER TO X INSIDE THE RADICAL THE GRAPH MOVED LEFT.

WHEN WE SUBTRACTED FROM X INSIDE THE RADICAL THE GRAPH MOVED RIGHT.

WHEN WE ADDED A NUMBER TO THE OUTSIDE OF THE RADICAL THE GRAPH MOVED UP AND WOULD MOVE DOWN IF WE HAD SUBTRACTED

Consider the following EQUATIONS, make a table, plot the points, and graph what you think the graph looks like.

11.  $f(x) = \sqrt[3]{x}$

x	y
-8	$\sqrt[3]{-8} = -2$
-4	$\sqrt[3]{-4} \approx -1.59$
-1	$\sqrt[3]{-1} = -1$
0	$\sqrt[3]{0} = 0$
1	$\sqrt[3]{1} = 1$
4	$\sqrt[3]{4} \approx 1.59$
8	$\sqrt[3]{8} = 2$

12.  $f(x) = 3\sqrt[3]{x}$

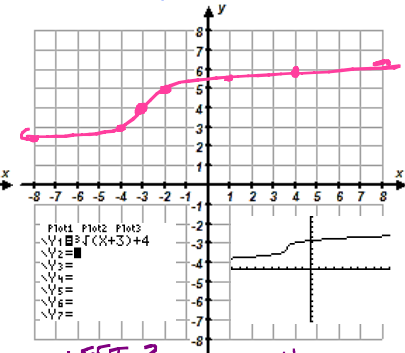
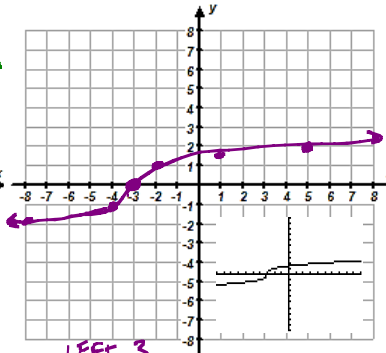
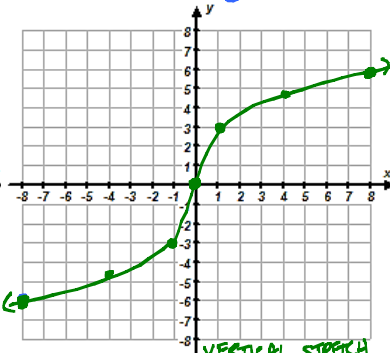
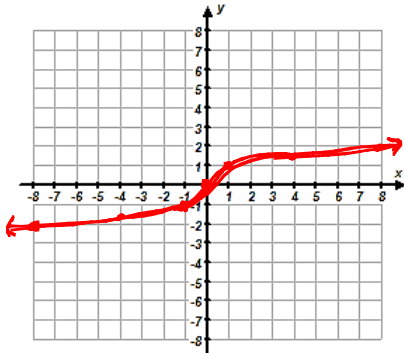
x	y
-8	$3\sqrt[3]{-8} = -6$
-4	$3\sqrt[3]{-4} \approx -4.76$
-1	$3\sqrt[3]{-1} = -3$
0	$3\sqrt[3]{0} = 0$
1	$3\sqrt[3]{1} = 3$
4	$3\sqrt[3]{4} \approx 4.76$
8	$3\sqrt[3]{8} = 6$

13.  $f(x) = \sqrt[3]{x+3}$

x	y
-8	$\sqrt[3]{-8+3} \approx -1.71$
-4	$\sqrt[3]{-4+3} = -1$
-3	$\sqrt[3]{-3+3} = 0$
-2	$\sqrt[3]{-2+3} = 1$
1	$\sqrt[3]{1+3} \approx 1.59$
5	$\sqrt[3]{5+3} = 2$
8	$\sqrt[3]{8+3} \approx 2.22$

14.  $f(x) = \sqrt[3]{x+3} + 4$

x	y
-8	$\sqrt[3]{-8+3} + 4 \approx 2.29$
-4	$\sqrt[3]{-4+3} + 4 = 3$
-3	$\sqrt[3]{-3+3} + 4 = 4$
-2	$\sqrt[3]{-2+3} + 4 = 5$
1	$\sqrt[3]{1+3} + 4 \approx 5.59$
5	$\sqrt[3]{5+3} + 4 = 6$
8	$\sqrt[3]{8+3} + 4 \approx 6.22$



15. Sketch a graph of  $f(x) = 2\sqrt{x+3} - 4$  and answer the following questions.

a. Explain the transformations of the parent function  $p(x) = \sqrt{x}$  to create  $f(x)$ .

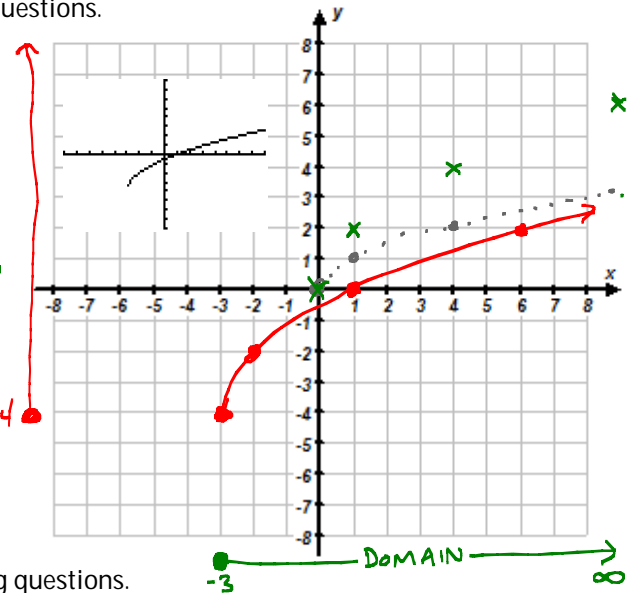
VERTICAL STRETCH FACTOR 2  
LEFT 3, DOWN 4

b. Domain of  $f(x)$ :  $x \geq -3$  SET NOTATION  $[-3, \infty)$  INTERVAL NOTATION

c. Range of  $f(x)$ :  $y \geq -4$  SET  $[-4, \infty)$  INTERVAL

d. End Behavior of  $f(x)$ : AS  $x \rightarrow -\infty$  (LEFT)  $f(x) \rightarrow$  UNDEFINED  
AS  $x \rightarrow \infty$  (RIGHT)  $f(x) \rightarrow \infty$  (UP)

e. Extrema: A MINIMUM AT  $(-3, -4)$



16. Sketch a graph of  $g(x) = -3\sqrt[3]{x+4} + 2$  and answer the following questions.

a. Explain the transformations of the parent function  $p(x) = \sqrt[3]{x}$  to create  $g(x)$ .

• REFLECT OVER X-AXIS & VERTICAL STRETCH FACTOR 3  
• LEFT 4  
• UP 2

b. Domain of  $f(x)$ : ALL REALS (R)  $(-\infty, \infty)$

c. Range of  $f(x)$ : ALL REALS (R)  $(-\infty, \infty)$

d. End Behavior of  $f(x)$ : AS  $x \rightarrow -\infty$  (LEFT),  $g(x) \rightarrow \infty$  (UP)  
AS  $x \rightarrow \infty$  (RIGHT),  $g(x) \rightarrow -\infty$  (DOWN)

